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DOI:

[10.1039/C9SC01135H](https://doi.org/10.1039/C9SC01135H)

Document Version

Peer reviewed version

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Citation for published version (APA):

Abbasi Perez, D., Sang, H., Perez-Garcia, L., Floris, A., B. Amabilino, D., Raval, R., Manuel Recio, J., & Kantorovitch, L. (2020). Controlling the preferential motion of chiral molecular walkers on a surface. *Chemical Science*, 10(23), 5864-5874. <https://doi.org/10.1039/C9SC01135H>

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Controlling preferential motion of chiral molecular walkers at a surface

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9th May 2019

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Abstract

Molecular walkers standing on two or more “feet” on an anisotropic periodic potential of a crystal surface may perform a one-dimensional Brownian motion at the surface-vacuum interface along a particular direction in which their mobility is the largest. In thermal equilibrium the molecules move with equal probabilities both ways along this direction, as expected from the detailed balance principle, well-known in chemical reactivity and in the theory of molecular motors. For molecules that possess an asymmetric potential energy surface (PES), we propose a generic method based on the application of a time-periodic external stimulus that would enable the molecules to move preferentially in a single direction thereby performing as Brownian ratchets. To illustrate this method, we consider a prototypical synthetic chiral molecular walker, the 1,3-bis(imidazol-1-ylmethyl)-5(1-phenylethyl)benzene, diffusing on the anisotropic Cu(110) surface along the Cu rows. As unveiled by our kinetic Monte Carlo simulations based on the rates calculated using *ab initio* density functional theory, this molecule moves to the nearest equivalent lattice site via the so-called inchworm mechanism in which it steps first with the rear and then with the front foot. As a result, the molecule diffuses via a two-step mechanism, and due to its inherent asymmetry, the corresponding PES is also spatially asymmetric. Taking advantage of this fact, we show how the external stimulus can be tuned to separate molecules of different chirality, orientation and

conformation. The consequences of these findings for molecular machines and the separation of enantiomers are also discussed.

1 Introduction

The controlled movement of molecules, either through intramolecular switching or binding and release between molecules, is a challenging contemporary goal. Hence, development of novel methods for controlling molecular motion on surfaces is necessary. The related area of research known as molecular motors[1, 2, 3, 4, 5, 6, 7] has also become a topic of significant interest. These molecular motors (or machines) under certain conditions are capable of a net unidirectional motion. In biology motor proteins such as kinesin[8, 9, 10], myosin[11] or dynein[12] “walk” along one-dimensional tracks thereby performing specific tasks in the cells. Inspired by these biological systems, successful DNA track nano-walkers have been developed[13, 14, 15]. The behaviours of many other molecules have also been investigated in terms of their ability to walk or rotate preferentially in a particular direction either driven by a laser pulse[16], chemical reactions[17, 18, 19, 20], electric field[21, 22, 23, 24], temperature[25], or a combination of different stimuli[26]. A ratchet-like behaviour has been observed in colloidal particles[27], an artificial motor system designed to replicate a realistic motor protein[28], cold atoms in optical lattices[29, 30, 31], nanoparticles in solution[32, 33], in SQUIDs[34], soliton transport[35], nanopores in polymer films[36], polarons in diatomic molecular chains[37], superparamagnetic particles[38], and many other cases.

Fundamental principles leading to unidirectional motion of molecules are well understood[39, 40, 41, 42, 43, 2]. If in thermal equilibrium a Brownian particle is placed in a periodic potential of a lattice in a single dimension 1D (which could be achieved, e.g., on surfaces with strong anisotropy, such as the Cu(110) surface [44]), then it would diffuse on average equally likely in both directions along that dimension even though the corresponding potential energy surface (PES) may consist of asymmetric periodic parts (or waveforms). This is because at equilibrium the principle of detailed balance is at work not allowing a net mass transport in any particular direction without doing any work (since that would contradict the second law of thermodynamics). In order to enforce unidirectional mass transport, one has to break thermal equilibrium. This can be achieved by applying an external stimulus, e.g. an external field or temperature fluctuation, or, as it is the case in biological systems, by performing a work on the molecules via a chemical reaction. Alongside the application of a time-periodic stimuli (e.g. a field or temperature gradient), an additional condition of broken symmetry is required. For instance, for a unidirectional movement the PES must consist of asymmetric periodic waveforms.

Our main objective is to propose a method based on applying external time-periodic stimulus which would enable one to enforce preferential motion of molecular walkers. As an illustration of our method and a proof of principle, in this paper we explore the Brownian motion of a realistic small bipedal molecule 1,3-bis(imidazol-1-ylmethyl)-5(1-phenylethyl)benzene (BIPEB), see the inset in Fig. 1, on the Cu(110) surface. Alongside the most

stable geometry, a different conformer is also considered that is slightly less stable. This surface consists of parallel rows of protruding Cu atoms making it highly anisotropic. Consequently the molecules diffuse mostly along the rows; this is similar to a small molecular walker considered previously [44] that encounters much higher diffusion barriers across the rows than along the rows. The molecules diffuse along the rows by stepping separately with the rear “foot” and then with the front one akin to the inchworm mechanism, [44] and yielding a PES consisting of two-barrier periodic waveforms with barriers of different height, i.e. these waveforms lack spatial symmetry.

The plan of the paper is as follows. In the next section we shall briefly consider the computational methods employed. Then the molecules are introduced and their PES calculated and discussed in Section 3.1. In Section 3 results of the kinetic Monte Carlo simulations without and with various static and time-periodic external stimuli are discussed. Finally, conclusions are drawn in Section 4.

2 Methods

The geometry of the molecules on the surface was relaxed using an *ab initio* density functional theory (DFT) method as implemented in the CP2K computer code[45], which uses Goedecker-Teter-Hutter (GTH) pseudopotentials to describe atomic core electrons, and a hybrid scheme based on both Gaussian orbitals and plane waves (GPW) as the basis set for valence electrons. Exchange-correlation interaction was described by the Perdew-Burke-Ernzerhof density functional[46], while the dispersion interaction by the rVV10 functional[47]. The energy cutoff used was 400 Rydberg. To perform these calculations we used a periodic slab of the Cu(110) surface containing 2 layers of Cu atoms with a vacuum gap of 13 Å (138 atoms altogether), with atoms of the upper layer allowed to relax. As our calculations serve to yield mostly a general qualitative picture, this number of layers is considered sufficient. The 9 x 5 lateral size of the periodic unit cell with a single molecule on its surface was chosen such that the interactions between molecular images are negligible. Only $\mathbf{k} = \mathbf{0}$ (Γ) point was used in our calculations. The geometry relaxation was stopped when the forces on atoms were less than 1 meV/Å.

To calculate the PES of the molecules associated with a single translation along the Cu rows between two equivalent lowest energy positions, the Climbing Image Nudged Elastic Band (CI-NEB)[48, 49] method was applied; in some cases the Dimer method[50] was used to optimise the geometry of the transition state. The path was split into two separate NEB simulations by an intermediate geometry found (see Section 3.2). The spring constant used varied between 2 and 5 eV/Å². The NEB calculations were considered converged when the maximum force on the atoms of the band was less than 10 meV/Å.

As for the computational tool used for investigating molecules’ dynamics we chose the kinetic Monte Carlo (KMC) method[51, 52] as a simple and practical alternative to the method based on the Fokker-Plank equation[2, 42], which has been widely used in studies on Brownian ratchets. This is because an application of the latter method to realistic many-atomic molecules is highly difficult due to many degrees of freedom the whole system possesses.

Moreover, when using the KMC method, we benefit from the advanced electronic structure methods, such as those based on DFT, and are able to calculate the corresponding transition rates. For these we have used the harmonic transition state theory (HTST)[51, 53] according to which the transition rate $r_{A \rightarrow B}$ between two states A and B is calculated via $r_{A \rightarrow B} = \nu \exp(-\beta\Delta)$, where ν is the frequency pre-factor, $\beta = 1/k_B T$ inverse temperature, k_B Boltzmann constant, and Δ the energy barrier. The pre-factors can in principle be calculated from the vibrational frequencies of the system in the minimum and the saddle point (transition state) using Vineyard formula[53]. However, as this calculation is rather expensive, it was performed only for one molecule (see SI), and then fixed pre-factors were chosen at the value of $\nu = 10 \text{ ps}^{-1}$ for all transitions, with or without the stimulus. This simplification should not affect our conclusions as the transition rates are exponentially more sensitive to the energy barriers rather than to the pre-factors.

Now we have to discuss how the energy barriers in the presence of a weak external stimulus were calculated. Two types of the stimuli we have in mind in this study: (i) a uniform external electric field E [21, 24], and (ii) a spatially uniform temperature gradient $g_T = \nabla T$ [25]. In the former case the molecule must be charged, and its PES would then be directly affected by the field causing the energy barriers to respond to it. Indeed, let E be the electrostatic field along the direction x of the Cu rows on the surface, measured in $\text{eV}/\text{\AA}$. The electrostatic potential across this direction, $V(x) = -Ex$, changes linearly with the distance and has to be added to the potential energy of the molecule calculated with DFT. As a result of this, the potential energy barriers $\Delta(x)$ of the transitions linearly change with x . Note that for this mechanism to work, it is not sufficient for the molecule to have only a dipole moment (e.g. due to a charge exchange with the metal surface), as in this case the contribution of the field to the PES will be spatially uniform and hence would not affect the energy barriers in a desired way. It is easy to see that the effect of the field is such that the barriers in the direction of the field are reduced, while in the opposite direction increased.

In the second case of the temperature gradient the PES is affected indirectly via an effective change of the energy barriers. Indeed, for constant gradients g_T , one has the temperature proportional to the distance x via $T(x) = T_0 + g_T x$, with T_0 being the temperature somewhere in the middle of a molecular track (we assume that these tracks are of finite lengths λ such that $|g_T \lambda| \ll T_0$). Then, the transition rate can be approximately written as

$$r_{A \rightarrow B} = \nu \exp \left[-\beta_0 \left(1 + \frac{g_T x}{T_0} \right)^{-1} \right] \simeq \nu \exp [-\beta_0 \Delta(x)]$$

where $\beta_0 = 1/k_B T_0$ (in all our calculations we used the same temperature $T_0 = 220 \text{ K}$) and we have introduced an effective (distance dependent) energy barrier $\Delta(x) = \Delta - \left(\frac{g_T \Delta}{T_0} \right) x$. The effect of this stimulus is that the effective energy barriers in the direction of the temperature gradient (assuming $g_T > 0$) are increased, while those in the opposite direction reduced. This change can also be approximately treated as being caused by an effective ‘electrostatic’ field $E_{eff} = \frac{g_T \Delta}{T_0}$ with Δ being some ‘average’ energy barrier.

Hence, both cases can be considered on the same footing, and in the following we shall interchangeably use both

words, the ‘stimulus’ and the ‘field’, depending on the context.

Since our main purpose in this study is to understand the qualitative effects of the time-periodic stimulus on the molecular ratchet, the following approximate method which mimics all the essential features of the realistic calculation, has been used. Since, due to the field E_{eff} the energy barriers change linearly with the distance x along the Cu rows on the surface and are increased in one direction and reduced in the opposite one, this can be imagined by the final PES of a molecule being tilted one or the other way, depending on the direction of the field. As the only meaningful quantities responsible for the net mass transport are the transition rates, it is sufficient to shift the energy barriers up/down by an appropriate amount (see Section 3.2 for details, especially Fig. 4(c)).

Finally, since in our simulations the external driving changes with time, additional care should be taken when running KMC simulations. This is because in the standard formulation of KMC it is assumed that the rates remain constant in time, which is obviously not the case in our simulations, where the rates depend on time due to the time dependent external stimulus modifying the energy barriers in real time. Therefore, we use here an approach [54] in which this assumption is lifted. At variance with the standard algorithm in which the rates for the system to jump into all available states from the given state are used and the timestep is chosen at random from the exponential distribution, in the method we used, the timestep Δt is fixed to 100 ps and *probabilities* to jump *as well as to remain* in the current state over this time are employed. Otherwise, the two algorithms are very similar.

3 Results

3.1 Isomers and their potential energy surface

The preferential directional motion of a synthetic walking molecule is an important goal which can be achieved in the minimalist walker molecule on the copper surface described here given two conditions: (i) selective and directional adsorption on the Cu(110) surface and (ii) the application of an external stimulus. This effect can be seen in its simplest case by considering the energy minimum structures of two enantiomers that when arranged with their “tails” along the same normal to the copper atom rows will present mirror image potential energy surfaces.

In this study, as a prototypical molecular walker, we consider an (electrically neutral) synthetic bipedal molecule 1,3-bis(imidazol-1-ylmethyl)-5(1-phenylethyl)benzene (BIPEB) shown in Fig. 1(a). We refer to different parts of the molecule as body, tail and legs, as indicated in the scheme; the body is the benzene group, while the tail (1-phenylethyl) and the legs (imidazol-1-ylmethyl groups) are attached to it. Within the legs, the imidazole are the feet. The molecule possesses a stereogenic carbon atom in its tail, shown as yellow, leading to the existence of two enantiomers, (*R*) and (*S*), Fig. 1(b); both adopt a 3D geometry in the gas phase. When placed on the Cu(110) surface, several adsorption geometries were found for either of the two (the geometries of (*R*) being mirror reflections of those of (*S*)), with the most energetically favourable structure shown for the (*S*) enantiomer in Fig. 1(c). The molecule is strongly bound to the surface with the binding energy of 3.61 eV (after inclusion of the basis

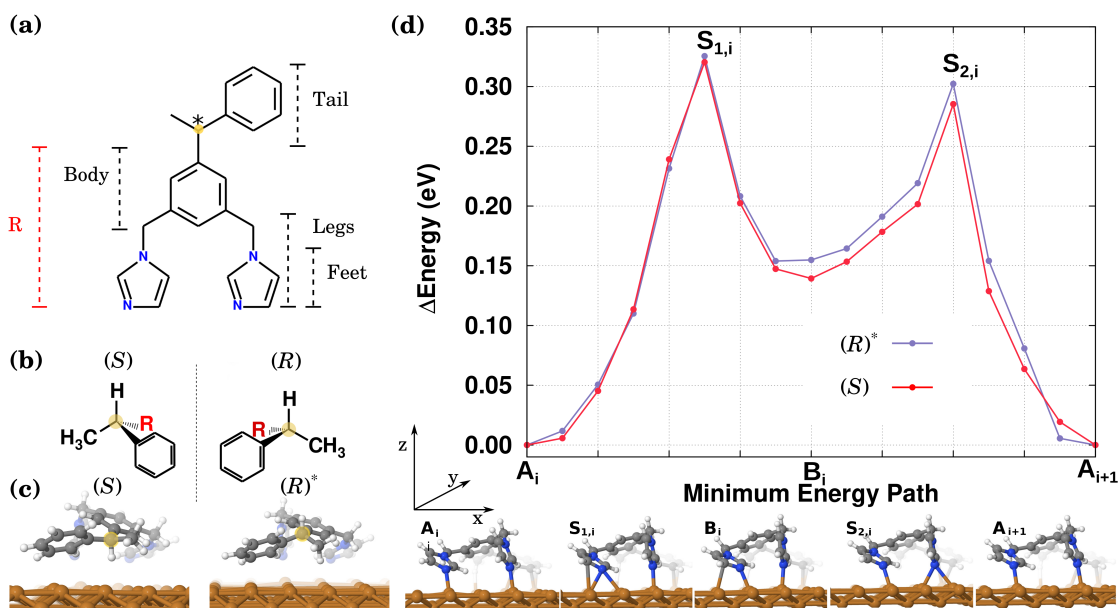


Figure 1: (a) BIPEB molecule. The chiral centre is highlighted in yellow. (b) The (*S*) and (*R*) enantiomers representation in their 3D projection. Dashed line indicates a mirror plane. (c) Two relaxed geometries considered here, as viewed from the tail to show the chiral centre (yellow). The shown geometry of (*S*) is the most energetically favourable. The considered relaxed geometry (*R*)*, that is related to enantiomer (*R*) as one of its conformers, is by 0.1 eV less stable than (*R*) (which mirrors (*S*) exactly), and hence represents a metastable structure. (d) Top: DFT CI-NEB calculated *change* of the PES of the two enantiomers, (*S*) and (*R*)* along the diffusion path. Bottom: a legs view of selected geometries (the minima and saddle points) of the (*R*)* enantiomer during its 1D diffusion along the Cu row. The (*S*) or (*R*)* molecules go through a set of equivalent geometries with the corresponding difference due to their centre of chirality as shown in (c).

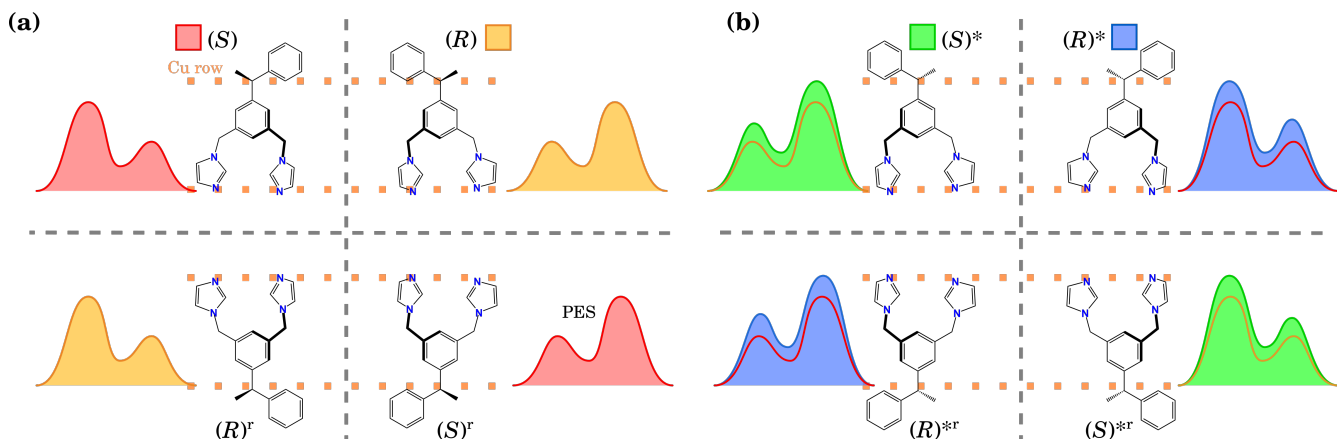


Figure 2: (a) Schematics (the top view) of the four most energetically favourable equivalent configurations the BIMPEB molecule can adopt when adsorbed on the surface, shown with the schematics of their corresponding PES. By symmetry, these four configurations have exactly the same energy. The four geometries are connected by mirror symmetry operations (grey dashed lines). Every reflection transforms the molecule into its enantiomer, but only the reflection over planes perpendicular to the Cu rows also transforms the PES by reflecting it. The rotated configurations (bottom line) (*S*)^r and (*R*)^r are equivalent to the (*S*) and (*R*) enantiomers, respectively, and are obtained by a 180° rotation about the axis perpendicular to the surface. (b) Conformers and their PES shown in filled colour. For comparison, we also show with the line of appropriate colour the PES of the corresponding competitive molecule from (a), which has the closest PES shape (but slightly different barriers). This colour code for each isomer is used throughout the paper: red, yellow, green and blue will represent the isomers (*S*), (*R*), (*S*)* and (*R*)*, respectively. Note that for clarity the schematic PES shown here do not correspond exactly to the calculated ones shown in Fig. 1(d).

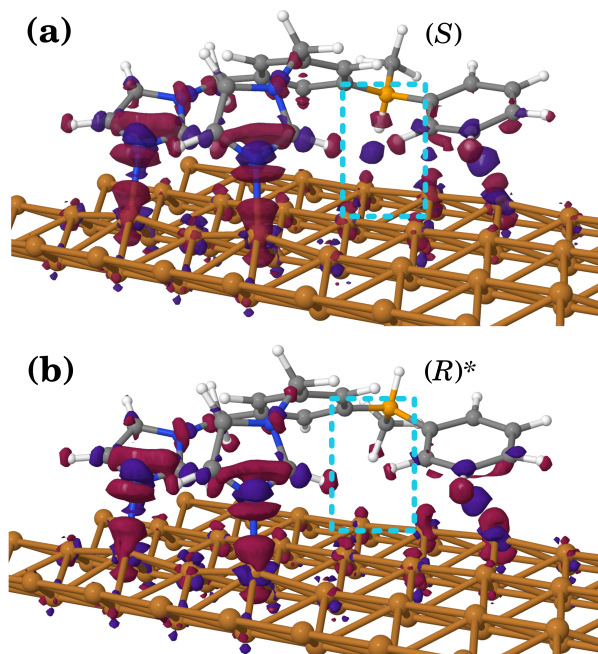


Figure 3: Comparison of the electronic density difference maps between the (*S*) (a) and (*R*)* (b) conformers of the BIPEB molecule adsorbed on the Cu (110) surface. Red (negative) and purple (positive) isosurfaces correspond to ± 0.003 electron/ \AA^3 . White, grey and blue balls stand for H, C and N atoms, respectively. The orange ball represents the stereogenic carbon atom, responsible for the different orientations of the methyl group and of the H atom of the enantiomers on the surface. The region where the interaction of the molecule with the surface differs is highlighted by the cyan dashed boxes.

set superposition error (BSSE) employing the counterpoise method[55]).

Here we also consider a competitive geometry that, as compared to (*S*), has the H atom and the methyl group attached to the stereogenic carbon swapped with each other, which changes its chirality from (*S*) to (*R*). The H atom is pointing outwards the surface, while in (*S*) it is directed towards it (the methyl group in both cases is pointed in the opposite direction to that of the H atom). Therefore, this metastable geometry is to be considered as another conformer of the (*R*) enantiomer, and will be referred to hereafter as the conformer (*R*)*, Fig. 1(c). It is 0.1 eV less stable than the (*S*) or (*R*) geometries. It is important to note that the calculated energy difference of 0.1 eV between the two conformers (*R*) and (*R*)* (and similarly between (*S*) and (*S*)*) is due to the existence of the stereogenic centre in the BIPEB molecule. The three point model for binding describes this situation well, and is a consequence of the “handedness”, or rather “footedness”[56] of the molecule.

These two conformations can generate other equivalent geometries related by mirror symmetry due to a plane perpendicular to the surface. This symmetry operation does not change the absolute value of the energy, but can change the shape of the PES. The mirror reflection of the (*S*) enantiomer with respect to a plane perpendicular to the Cu row leads to the (*R*) enantiomer. This operation also mirrors the PES. If the mirror plane is parallel to the Cu row, we transform the (*S*) enantiomer into the (*R*), but this time the tail points towards the opposite direction. We call this the (*R*)^r enantiomer, as it is equivalent to rotating the enantiomer (*R*) by 180° with respect

to an axis perpendicular to the surface. This operation does not change the shape of the PES. Hence, enantiomers (S) and (R) have identical orientations but mirrored PES, while enantiomers (S) and (R)^r have identical PES but different orientations. The same procedure can be applied to the (R)^{*} conformer. Due to these symmetry relations, calculating the PES only for one enantiomer and one of its conformers allows us to obtain the PES for the rest of the geometries. All eight conformations are presented in Fig. 2, with their corresponding PES to show how it is modified after each reflection.

In all geometries, the BIPEB molecule shows two N-Cu interactions[44] similar in nature to the nitrogen atom surface (NAS) interactions we have recently reported for the p-terphenyl m-dicarbonitrile molecule on the Ag (111) surface[57]. This is clearly seen in the electron density difference (EDD) maps shown in Fig. 3. The imidazole groups of the molecule interact with the surface via their nucleophilic nitrogen atoms that act as its feet, which bind to two non-adjacent Cu atoms in the same close-packed row. The NAS interactions are strong enough to noticeably lift up the interacting Cu atoms from their relaxed positions on the surface. At the same time, the tail of the molecule interacts with a neighbouring Cu row; however, this binding is much weaker than that of the imidazole feet as the EDD maps illustrate and hence this connection to the surface is less important and in most cases can be ignored, except when the two geometries are compared with each other as we discuss below. Comparing the EDD of (S) and (R)^{*}, we can see that the (S) enantiomer has an extra interaction with the surface via the H atom attached to the stereogenic C, which is missing in the (R)^{*}. This interaction appears in the EDD in a “kebab”-like form, i.e. via alternating regions of excess and depletion of the electronic density along the straight line connecting the atoms participating in the bond, and is highlighted in Fig. 3. This fact yields slightly different barrier heights for both geometries along the asymmetric PES, which will be exploited later on for their separation.

In the stable equilibrium geometries for both (S) and (R)^{*} the imidazole feet are separated by a single Cu atom along the same row. We have also found another adsorption geometry for both conformers in which there are no Cu atoms between the feet, see geometry B_{*i*} at the bottom of Fig. 1(d). This configuration is 0.15 eV less favourable and appears as an intermediate state between the more stable equilibrium geometries labelled A_{*i*}, A_{*i*+1} (see below). Note that other adsorption geometries are also possible when both feet stand on the neighbouring Cu rows or the tail is rotated. However, these are much less favourable and hence are much less relevant in considering the molecules diffusion and will be ignored hereafter.

To calculate the diffusion path between the two most favourable geometries of Fig. 1(c), we first run NEB calculations between these two states via two different mechanisms: one, in which the molecule slides as a whole along the Cu row in a one-step motion, and the other, the so-called inchworm mechanism, in which the molecule follows a two-step movement whereby first its rear foot moves forward and then its front one. Interestingly enough, the latter calculation indicated the existence of an intermediate minimum in the middle of the path. After relaxation of the geometry in that minimum, the second geometry mentioned above (labelled B_{*i*} at the bottom of Fig. 1(d)) was found. Hence, the whole path was split into two, and two separate CI-NEB simulations were run with 9 images

Description	Δ (eV)	
	$(R)^*$	(S)
From A_i to B_i (to the right)	0.339	0.320
From A_{i+1} to B_i (to the left)	0.316	0.285
From B_i to A_{i+1} (to the right)	0.147	0.146
From B_i to A_i (to the left)	0.170	0.181

Table 1: Energy barriers Δ for the diffusion of the two conformers by one lattice constant along the Cu row. See the bottom of Fig. 1(d) for labels A_i , B_i and A_{i+1} .

each, to characterize both elementary steps. This computational scheme was applied to both the (S) and $(R)^*$. The resulting PES for the complete inchworm path between two equivalent states (A_i , A_{i+1}) that passes through an intermediate minimum B_i , is shown at the top of Fig. 1(d) for both enantiomers. A selection of geometries along the path of $(R)^*$ is shown at the bottom. The PES for the other molecules can be obtained by applying the corresponding symmetry operations, as shown in Fig. 2. While the NEB calculation for the sliding mechanism revealed a one-step diffusion with the energy barrier of 0.55 eV, in the inchworm mechanism the diffusion occurs via a two-step diffusion path where the highest barrier was found to be below 0.34 eV. Hence, it is evident that the diffusion of either of the molecules is manifested by the inchworm walking mechanism [44], whereby imidazole groups act like feet that step on top of the Cu atoms along the row: to move forward, first the rear foot moves one surface lattice constant ($A_i \rightarrow B_i$), then the front foot moves forward one lattice constant ($B_i \rightarrow A_{i+1}$) bringing the molecule to an equivalent state displaced by one lattice constant.

Thus, the PES of the two conformers in moving by one lattice constant along the Cu row is a waveform consisting of two peaks. In both cases the peaks heights, measured from the geometries A or B, are slightly different rendering the expected diffusion of the two conformers to be slightly different as well. This difference originates in the slightly different interaction of the tails of the two molecules with the surface. The calculated energy barriers between the minima are shown in Table 1 and are found to be indeed different by around 19 meV from A_i to B_i and 31 meV for A_{i+1} to B_i , for both conformers. Therefore, the PES of the molecules along a Cu row consists of an infinite periodic sequence of such two-peak waveforms. We conclude that the PES of either of the molecules is spatially asymmetric, even though the difference in peaks heights is small.

In performing KMC simulations, a periodic sequence of states A and B was in all cases considered with all possible transitions between neighbouring states. When a molecule moves the whole lattice constant to the right, i.e. $A_i \rightarrow B_i \rightarrow A_{i+1}$, then +1 (in units of the lattice constant) is added to its position along the row; when the molecule moves the whole lattice constant to the left, i.e. $A_{i+1} \rightarrow B_i \rightarrow A_i$, then -1 is added to its position, see Fig. 1(d).

A final note is in order related to the fact that when performing NEB simulations the molecule was not charged: the above calculation (and the dynamic simulations described in the following sections) corresponds directly only to the case of the temperature gradient as the stimulus. One may think that the PES calculated in our NEB simulation is irrelevant then to the first type of the stimulus, an external electric field, since in this case the molecule has to

possess a charge. We argue that even in this case the NEB calculation makes perfect sense, at least qualitatively. Indeed, the two-peak PES of the molecule is related primarily to the fact that the molecule stands on two ‘feet’ and diffuses via the inchworm mechanism. An extra charge on the molecule does not affect the former point (see the SI), and hence the latter point must be valid as well as a consequence. Therefore, if the molecule is charged, the energy barriers would somewhat change numerically; at the same time, the dynamical behaviours we obtain will remain qualitatively exactly the same.

3.2 Diffusion with zero and constant external stimulus

Consider first the diffusion of all conformers without being driven by any external field. The position of the molecules along the Cu row during the course of a selected number of KMC simulations is shown in Fig. 4(a). One can clearly see that there is no preference for the molecules to go in one or the opposite direction in spite of the fact that the waveform of their PES is asymmetric. After 50 ms, the average distance walked by the molecules is zero within the accuracy of our calculations.

The obtained results agree with the fundamental principle of the detailed balance (following from the second law of thermodynamics) that at thermal equilibrium there should be no such preference[40, 42, 43, 2]. In order for the molecules to move preferentially in a single direction, one has to break the *equilibrium* condition, e.g., by applying an external field or temperature gradient. In what follows, the latter method will directly be exploited, although, as was said above, qualitatively our simulations are valid for the former method as well.

In Fig. 4(b) calculated KMC paths are shown for the equally oriented enantiomers under constant values of the field $E_{eff} = \pm 0.02$ eV/ a , where $a = 2.56$ Å is the Cu-Cu distances along the Cu row. As expected, an application of a constant field forces the molecules to perform preferentially unidirectional movement in the direction of the field. Note that all conformers would move preferentially along the field. Moreover, each enantiomer may adopt two orientations on the same Cu row, the second being obtained from the first by rotating the molecule by 180° about the vertical axis. Because either of the PES is tilted in the same direction (either to the right or left, depending on the sign of E_{eff}), preferential diffusion along the field is observed irrespective of the orientation of the molecules, so the separation is difficult in this case.

Application of a permanent field along one direction of the copper rows will lead to motion of the molecules, but because of the differences in the potential energy surfaces the (*R*) and (*S*) enantiomers will move at different velocities, i.e. the distance travelled per certain time is actually different when going to the right (positive distance values) or to the left (negative distance values), Fig. 4(b). Indeed, if we look at the curves for the enantiomers (*S*) and (*R*), red and yellow respectively, the (*S*) molecule moves to the right ($E_{eff} > 0$) slower than the (*R*); in the case of the opposite direction of the field (to the left, $E_{eff} < 0$) the (*S*) moves faster than the (*R*): after 50 ms (*S*) travels around 17500 lattice constants to the right and 26000 lattice constants to the left, while the (*R*) travels 26000 lattice constants to the right and 17500 to the left. This can be explained in the following way. Suppose one

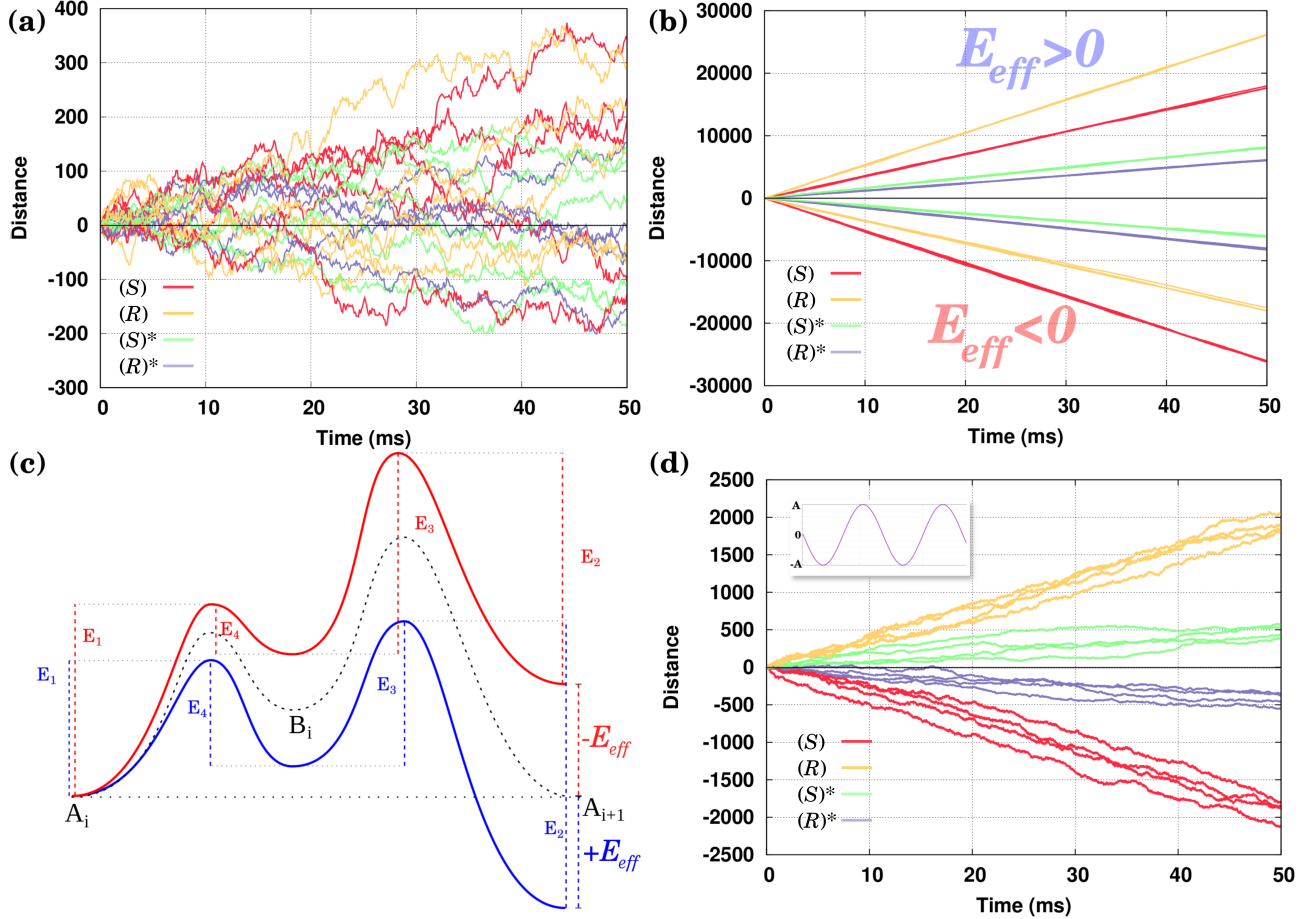


Figure 4: A set of KMC trajectories for all isomers with the same orientation (with each colour corresponding to different isomers) calculated (a) without external driving, (b) using the constant fields $E_{eff} = 0.02$ eV/ a , when all isomers move in the positive direction, and $E_{eff} = -0.02$ eV/ a , when they move in the negative direction, (d) using an oscillating external driving $E_{eff}(t) = A \sin(\omega t)$ ($A = 0.02$ eV/ a and $\omega = 10000$ s $^{-1}$). The inset in (d) shows the shape of the external field. In all cases the distance is measured in the integer number of the Cu-Cu distances $a = 2.56$ Å along the Cu row. (c) Schematics of the PES of the (R) molecule with and without the applied external effective field (stimulus): no field (the dashed line), with the positive field, $E_{eff} > 0$ (blue), and the negative field, $E_{eff} < 0$ (red). Under an electric field the PES is tilted one way or another, depending on the field direction, as shown. When the temperature gradient is applied, the PES does not change; however, the temperature gradient modifies the (effective) energy barriers in the same way as the electric field, see Section 2.

direction of the field forces the molecules to move preferentially along the field and in that direction the smaller peak of the PES comes first, while the opposite direction of the field makes the molecules preferentially to move in the opposite direction when the higher peak of the PES comes first. In this case the molecules would move faster in the former case than in the latter since overcoming a sequence of two smaller barriers ($A_{i+1} \rightarrow B_i \rightarrow A_i$) is on the whole ‘easier’ than moving in the opposite direction, $A_i \rightarrow B_i \rightarrow A_{i+1}$, which requires first climbing a larger energy barrier, Fig. 4(c).

Even though the application of the constant field cannot be used for molecular separation (molecules go all together displaying almost identical trajectories in each case, albeit with different speeds), the effect of the sign of the field on the velocity of the molecules in performing unidirectional movement appears to be crucial for developing methods which are capable of achieving the desired separation of the molecules via their unidirectional motion.

3.3 Separation of molecules using oscillating fields

We have seen that an application of a constant field (stimulus) is trivially able to cause unidirectional diffusion of the molecules along the field; because of the asymmetry of the PES, the speed with which the molecules move depends on the direction of the field. This effect can now be exploited in order to propose an external stimulus that is able to separate the molecules with respect to their *chirality* on the Cu rows. Note that the PES of an enantiomer is obtained simply by mirroring the PES corresponding to the original molecule, see Fig. 2. This is also true for molecules rotated by 180° .

The idea is to apply a time-periodic (but still spatially uniform) external field $E_{eff}(t) = A \sin(\omega t)$. In this case for any sensible choice of the parameters A and ω molecules of different chirality will move in the opposite directions and with the same speed, as shown in Fig. 4(d). Indeed, if in the case of a constant field molecules moved in the direction of the field, when applying an oscillatory field, molecules move preferentially in the direction in which they move faster (see our discussion above). As the enantiomer (S) moves faster to the left and the (R) to the right in the presence of a field, the application of an oscillating field will drive the enantiomers (S) to the left and the (R) to the right, performing a separation of enantiomers. Moreover, in the case of the molecules of opposite orientations their movement will be also mirror reflection of each other. Note that the actual trajectories shown in Fig. 4(d) are not exactly the mirror images of each other as they represent a sample of stochastic KMC trajectories.

Hence, applying a properly adjusted oscillating field, in a racemic mixture *with equally oriented molecules*, one should be able to separate the enantiomers. On the other hand, in a enantiopure system, it is possible to separate the molecules based on their orientation.

3.4 Separation of competitive conformers

As shown in Fig. 4 (d), both conformers (S) and (R)* (or (R) and (S)*), at least for the molecules considered here, would move in the same direction; only their velocities will be different. Hence, the oscillating field considered so

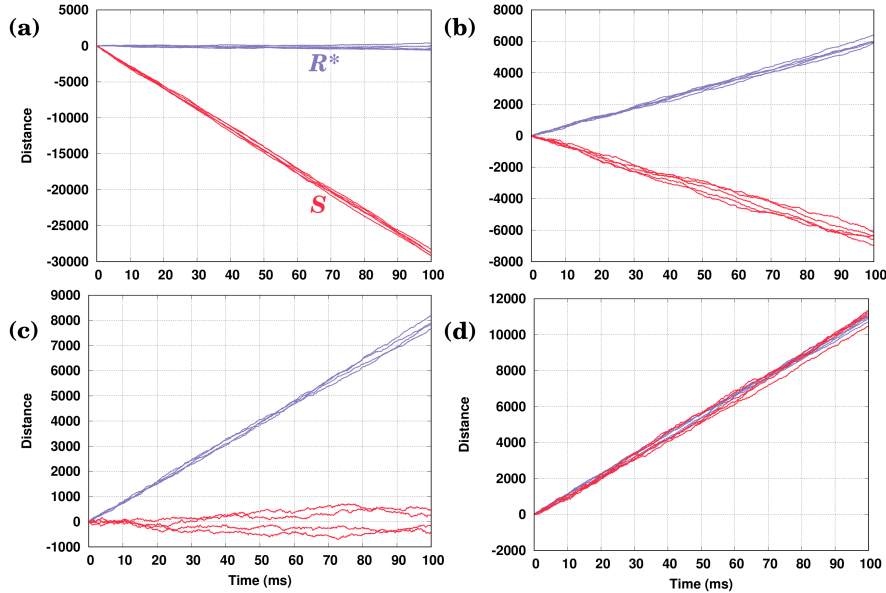


Figure 5: KMC trajectories for two conformers of identical orientation, $(R)^*$ (blue) and (S) (red), for several values of the shift parameter of the asymmetric external driving field: (a) $\delta = 0.021118$ (b) $\delta = 0.026411$; (c) $\delta = 0.02800$; (d) $\delta = 0.030818$. In all cases $A = 0.10$ eV/ a and $\omega = 10000$ s $^{-1}$. The distance is measured in the integer number of the Cu-Cu distances $a = 2.56$ Å along the Cu row.

far is not appropriate to separate them. This is because the field has equal duration in both positive and negative directions. In other words, a time-symmetric stimulus does not allow one to fully resolve the molecules of different conformations. In order to separate two competitive geometries (conformers with similar PES but slightly different energy barriers), it is necessary to allow for the field to operate in one direction longer (shorter) than in the other, i.e. the time symmetry must be broken. This asymmetry of the field can be easily created by applying, e.g., a shifted field, $E_{eff}(t) = A[\sin(\omega t) + \delta]$, where the relative displacement $-1 \leq \delta \leq 1$. By properly fine-tuning the parameters of the field, it is possible to exploit the difference in the conformers velocities. We can either make one conformer to stay around the initial position while the other moves away, Fig. 5(a,c), or make them to move with the same velocity, Fig. 5(d). Finally, we can make them to move in the opposite directions, i.e. to separate them, as shown in Fig. 5(b). Note that by taking the value of the parameter δ around the value used in Fig. 5(d), one can make the two molecules to move in the same direction, but with different velocities (not shown).

Hence, by applying a properly shifted (asymmetric) field it is possible to separate out molecules of different conformations.

3.5 Fences

Brownian molecular motion on surfaces may be conditioned by the intrinsic features of the molecules, the anisotropy of the surface or the existence of natural barriers such as steps and/or local defects (e.g. impurities). Molecular fences, e.g. such as the filaments of porphyrins described in Ref. [44], provide realistic spatial constraints for the walkers, adding new possibilities to the resolution of racemic mixtures. In particular, these fences could be used as

a practical tool in collecting the molecules of either one orientation, conformation or, possibly, even chirality.

Now we shall describe our KMC simulations in which two infinite parallel fences were placed perpendicular to the Cu rows, and the molecules are placed between them. It was assumed in our KMC simulations that the molecules cannot move across the fences, but can ideally be reflected upon them. How the distance between these barriers affects the separation of the conformers, when external fields differed only by the value of the shift parameter δ are applied, is illustrated in Fig. 6. In Figs. 6 (a) and (c), with $\delta_2 = 0.021294$ and $\delta_4 = 0.02800$, respectively, the applied fields are able to fuel one of the conformers in less than two milliseconds to one fence, while the second conformer remains broadly distributed between the fences. Note, however, that for distant fences at long simulation times the second molecule would spend more of its time at the other fence, as it is still under the influence of the field that biases its movement, see right panels in Fig. 6(a,c). Applying a different field with $\delta_3 = 0.02638$, Fig. 6(b), the two conformers are fully separated by the top (R)* and bottom (S) fences, but due to the stochastic nature of the movement, molecules confined near one fence may still reach the opposite fence if the distance between them is not large enough, see the left panel in Fig. 6(b). Note that by increasing the frequency ω of the field, molecules can be confined at narrower spaces and kept separated between even closer placed fences (not shown). For our system, a distance between fences of around 600 lattice constants (the middle column in (a-c)) would allow to have five different states in the presence of the field, Fig. 6(d): (i) both conformers at the lower fence ($\delta_1 = -1$), (ii) the conformer (S) at the lower fence while the (R)* moves broadly within the confined space ($\delta_2 = 0.02194$), (iii) both conformers separated at opposite fences ($\delta_3 = 0.026380$), (iv) conformer (R)* confined at the upper fence while the (S) moves everywhere ($\delta_4 = 0.02800$), and finally, (v) both conformers are at the upper fence ($\delta_5 = 1$). Note that all of these states are achievable by just changing the δ parameter of the field. Simulations were run for long times, up to one second, and show that these states are stable in time as long as the field is kept. Obviously, when the field is switched off, all molecules move freely between the fences.

4 Discussion and Conclusions

In this work, we have explored the unidirectional motion of a prototypical molecular walker under an external time-periodic stimulus such as a weak uniform temperature gradient which acts as an effective uniform field linearly distorting the molecular PES. Our results must also be directly relevant to the other type of the stimulus, an external uniform electric field, although in this case the calculated parameters of the field that influence the unidirectional motion are expected to be numerically slightly different. Practical ways of charging molecules on surfaces are e.g. discussed in Ref. [58, 59].

The particular chiral molecule considered is the 1,3-bis(imidazol-1-ylmethyl)-5(1-phenylethyl)benzene that has two enantiomers, (R) and (S). We demonstrated that both enantiomers diffuse on the Cu(110) surface via a walking mechanism akin to the inchworm motion where the molecule's first step is with its rear foot and then with its

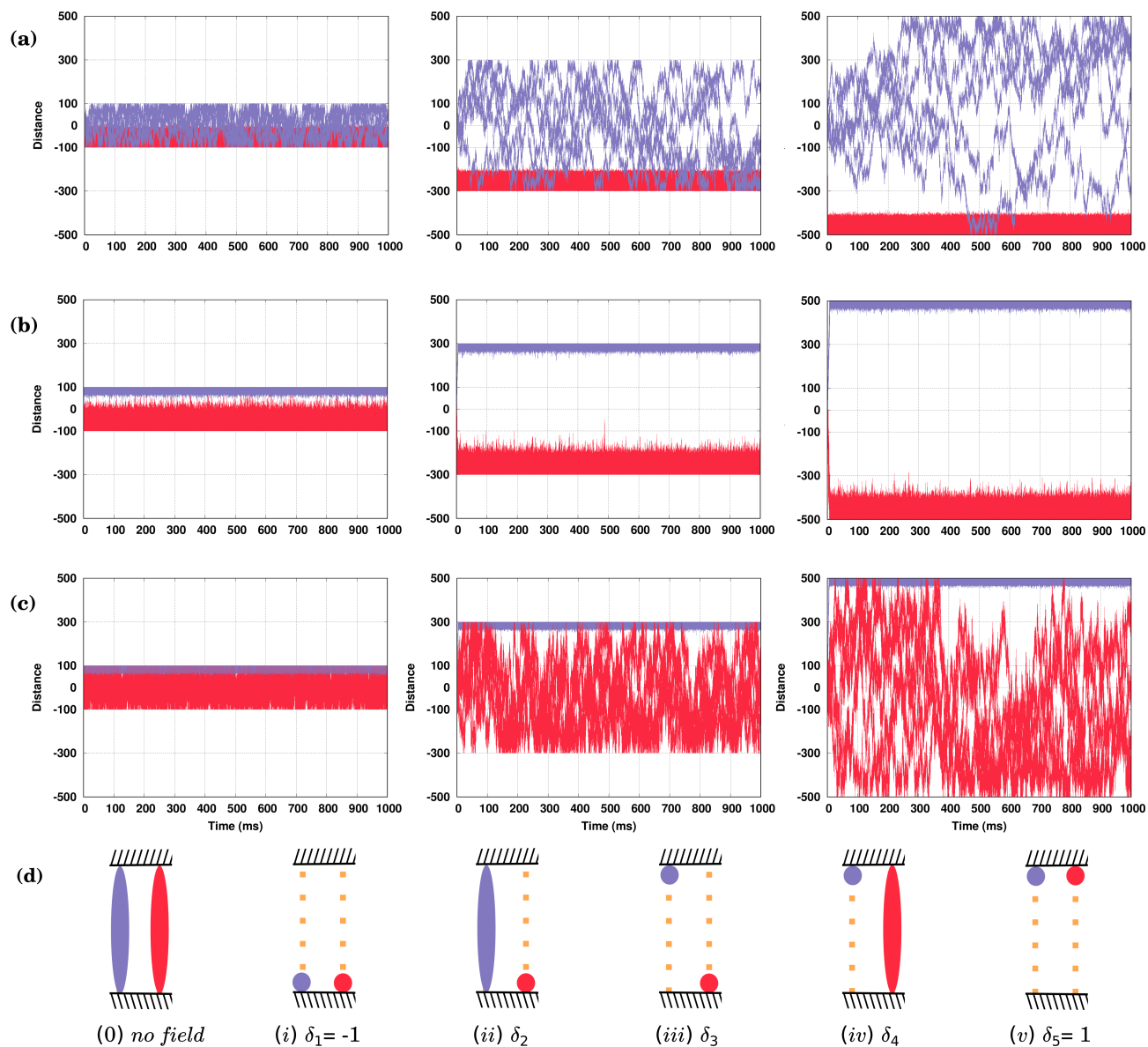


Figure 6: (a,b,c) KMC simulations of both conformers (R^* - blue, S - red) confined between two molecular fences oriented horizontally and spaced by 200 (left panels), 600 (middle) and 1000 (right) lattice constants under the effect of three different external sinusoidal fields with various displacement factors δ : (a) $\delta_2 = 0.021294$, (b) $\delta_3 = 0.026380$ and (c) $\delta_4 = 0.02800$. The ‘distance’ is measured in the integer number of the Cu-Cu distances $a = 2.56 \text{ \AA}$ along the Cu row. (d) Schematics of the time averaged spatial distributions of six different states a confined system of two molecules between fences (striped blocks) may adopt. The fences are perpendicular to Cu rows shown by the small orange-filled squares for clarity.

front one. Consequently, the PES of the molecule on the Cu(110) surface consists of a periodic sequence of slightly asymmetric waveforms containing two peaks each associated with the stepping of a single foot. At variance with common computational approaches in which Brownian molecular ratchets are studied using oversimplified molecular models by means of, e.g., the Fokker-Planck equation, we propose a method that is based on running KMC simulations. The obvious advantage of our theoretical approach is that it is able to consider dynamics of realistic systems (both molecules and surfaces) with adsorption geometries and diffusion rates calculated using modern *ab initio* methods.

It has been shown that despite the spatial asymmetry in the PES of the molecules, no preferential motion into a particular direction along the Cu rows is observed, which is in accord with the second law of thermodynamics and the principle of detailed balance. However, unidirectional motion is achieved by the application of an external field, and we have shown that small differences in the heights of the two peaks in the PES waveforms yield different diffusion velocities of the molecules on the surface, according to the sign of the field. The central result of this study is that, when applying a uniform time-periodic (sinusoidal) external field, the molecules diffuse preferentially towards the direction they move faster. This effect is general and would be applicable to a wide class of surface-molecule systems, being of principal importance for the separation of the molecules. If we have a racemic mixture, where all molecules are equally oriented in the same direction and hence have mirror symmetric PES, they will diffuse in opposite directions under the presence of the oscillating field. It is also possible to separate molecules of the same kind (i.e. in an enantiopure system) but of opposite orientation as they would preferentially diffuse in the opposite directions along the Cu rows, thereby ensuring their separation.

Hence, we have shown that the molecules can be separated according to either their chirality or their orientation by applying an appropriate external stimulus.

In reality, for a chiral molecule and the surface like the one we considered here, there will be four types of isomers on the surface after deposition (see Fig. 2): (*S*), (*R*), (*S*)^{*r*} and (*R*)^{*r*} (and this is also true for each conformer), all present in equal quantities. Therefore, by applying our method, we should be able to separate these molecules into two groups: (i) (*S*) and (*R*)^{*r*}, and (ii) (*R*) and (*S*)^{*r*}, which corresponds only to a partial separation. However, if in the presence of the same field the PES of the molecules in different orientations are different (e.g. by applying an extra weak field acting in the direction perpendicular to the direction of motion), then using an appropriate modification of our method it should be possible to perform full separation of the molecules both with respect to their chirality and orientation.

Furthermore, we have demonstrated that when the PES are not mirror-symmetric but have a similar shape with slightly different energy barriers, the diffusion direction of the molecules can still be controlled. By combining a constant field with an oscillating one, so that the times during which the field points in both directions are different, one can fine-tune the parameters of such a field to achieve various effects in the diffusion of the enantiomers. For instance, one can ensure that one enantiomer moves faster (slower) than the other while moving in the same

direction, or one would on average not move at all while the other moves. Most intriguingly, however, we have shown that one can also adjust the parameters of the field (its constant component) in such a way that two competitive molecules, when oriented in the same way on the surface, would move in opposite directions.

The possibility to control the movement of the molecules in a confined system, like between fences, can have potential applications at the nanoscale. It could be used as a tool for molecular control. If fences for example are not only physical barriers that only block the diffusion, but molecules or electrodes, or even individual entities that can perform an action according to the presence (or not) of the molecules, then, the application of the field could rearrange the molecules in that hypothetical device and trigger a certain response. If this is taken to a more complicated device, these molecules could act as information carriers or molecular relays, activated by the shape of the external fields if instead of an inert fence there is a nanodevice capable of triggering a reaction according to the presence or not of the molecules. Also, the possibility to control the diffusion at the molecular level, could allow to seed enantiopure regions on a surface to start growing enantiopure self-assembled monolayers.

Our findings open a way for enantiomer separation with exciting applications in physics and chemistry. Understanding molecular ratchets provides a novel route to designing efficient methods to separate various molecules, with particular relevance to racemic mixtures of enantiomers where preferential crystallization works sporadically [60]. In particular, we have shown that by providing parallel fences [44] perpendicular to the Cu rows, one can collect molecules of the same orientation and/or chirality near different fences.

We hope that this study will be useful to a wide community of physicists and chemists working in different areas related to studying molecules on surfaces and in the field of molecular motors and nanoscale devices. Furthermore, it may contribute to solving exciting questions like why proteins and, by extension, life are stereospecific. Maybe this relation between the directional motion and chirality could be part of the answer.

Acknowledgement

Via our membership of the UK's HEC Materials Chemistry Consortium, which is funded by EPSRC (EP/L000202, EP/R029431), this work used both the ARCHER UK National Supercomputing Service (<http://www.archer.ac.uk>) and the UK Materials and Molecular Modelling Hub for computational resources, MMM Hub, which is partially funded by EPSRC (EP/P020194). This research was supported by the UK EPSRC grant EP/J019844/1 and in part by EP/N023587/1. H. S. would like to thank the support from the National Natural Science Foundation of China (Grant No. 21603086) and China Scholarship Council (Grant No. 201608420186). J. M. R. thanks the Spanish MINECO and FICYT for financial support (Projects CTQ2015-67755-C2-2-R, FC-GRUPIN-IDI/2018/000177) and Universidad de Oviedo for a mobility grant to visit King's College London.

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